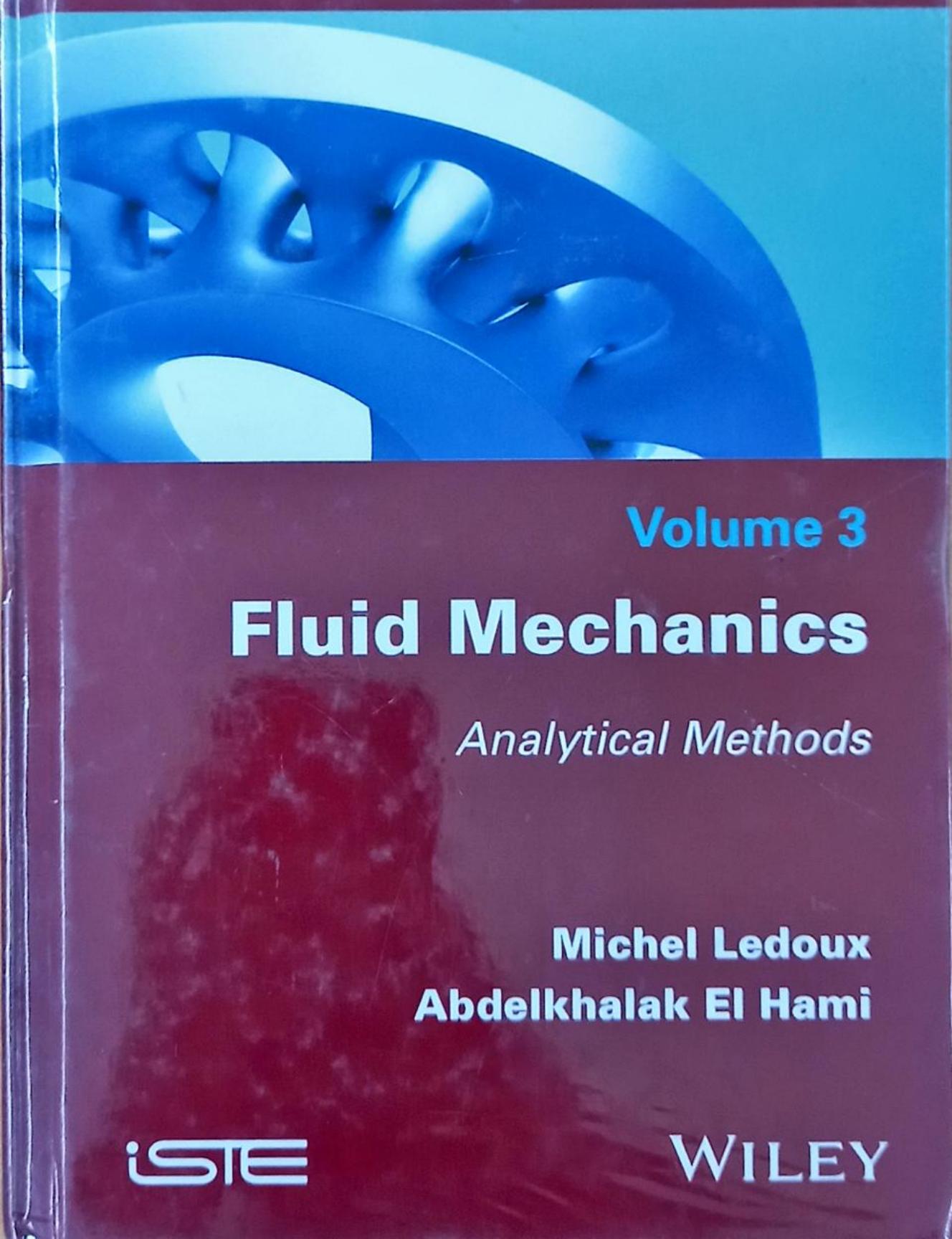


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**Volume 3**

# **Fluid Mechanics**

*Analytical Methods*

**Michel Ledoux  
Abdelkhalak El Hami**

**ISTE**

**WILEY**

Mathematical and Mechanical Engineering Set

coordinated by  
Abdelkhalak El Hami

Volume 3

# Fluid Mechanics

## *Analytical Methods*

Michel Ledoux  
Abdelkhalak El Hami

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Library of Congress Control Number: 2016959733

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British Library Cataloguing-in-Publication Data  
A CIP record for this book is available from the British Library  
ISBN 978-1-84821-951-9

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This book explores a variety of relatively simple approaches to academic and practical problems of fluid mechanics.

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