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METRIC VERSION

CALCULUS

OF A SINGLE VARIABLE

EARLY TRANSCENDENTAL FUNCTIONS

METRIC VERSION ■ 7TH EDITION



RON LARSON ■ BRUCE EDWARDS

CALCULUS OF A SINGLE VARIABLE

EARLY TRANSCENDENTAL FUNCTIONS

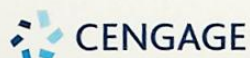
7e METRIC VERSION

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