THIRD EDITION

TEACHING MATHEMATICS IN THE SECONDARY SCHOOL

PAUL CHAMBERS AND ROBERT TIMLIN

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'This is a comprehensive guide covering everything about learning to teach maths. Suitable for anyone considering teaching as a profession, those already in training and new teachers, it provides excellent coverage of the theoretical and practical aspects of teaching maths in an accessible style.'

***EMMA McCREA, ITE LECTURER AND AUTHOR OF* MAKING EVERY MATHS LESSON COUNT**

This fully updated third edition is the perfect companion to help you succeed in training to teach mathematics in secondary schools. It looks at the fundamentals of mathematics teaching, how to plan lessons and assess learning and how to promote an inclusive approach in your classroom.

Key new features include:

- Updated content reflecting: the National Curriculum in England, the Teachers' Standards and revised requirements for GCSE and A level mathematics
- Updated 'Evidence from research' features, highlighting developments in the field
- An expanded section on mathematical misconceptions
- New coverage of teaching for mastery

This is essential reading for anyone undertaking initial teacher education courses in secondary mathematics, including university-based (PGCE, PGDE) and school-based (School Direct, SCITT, Teach First) routes into the profession.

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