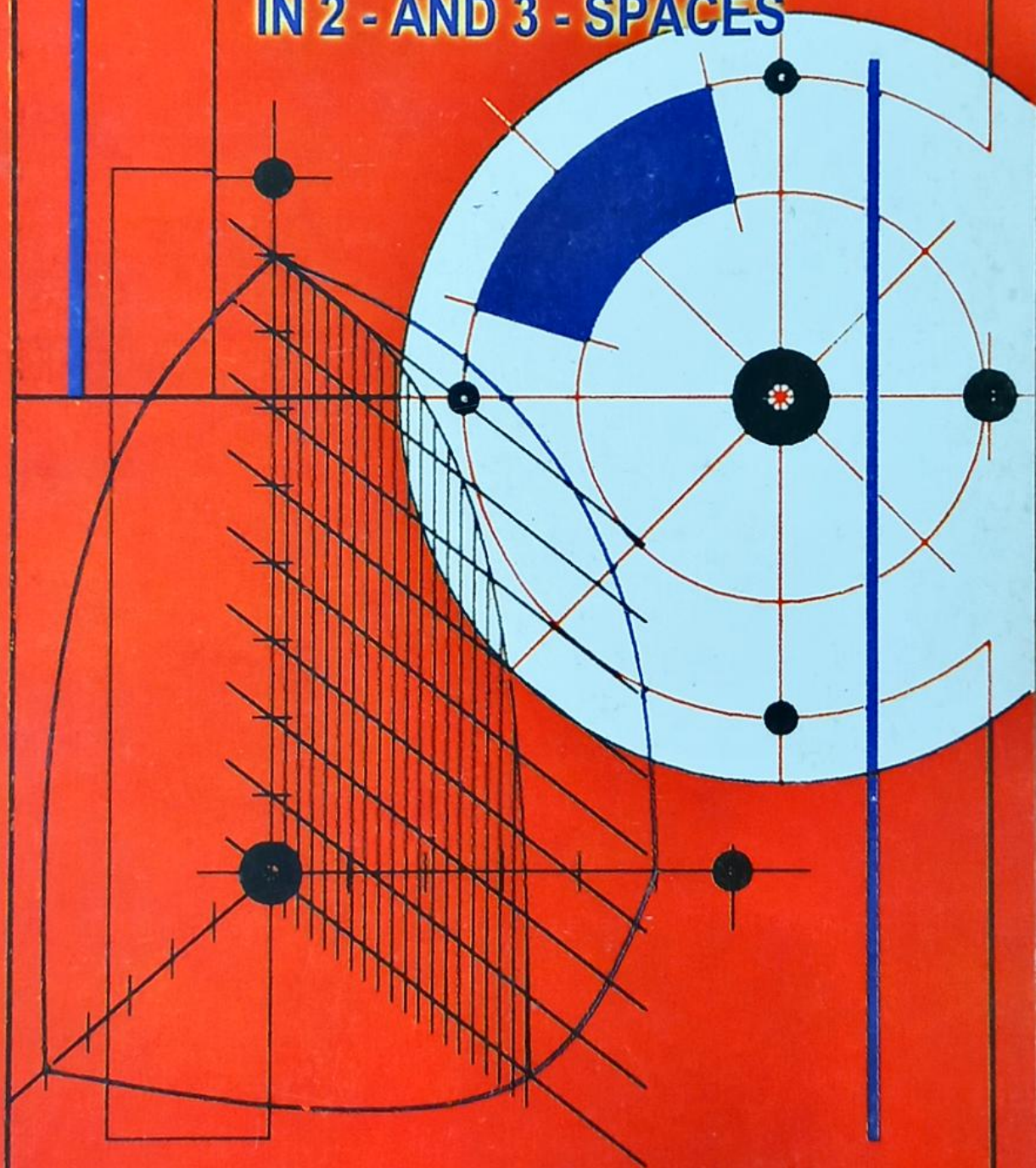
ANALYTIC GEOMETRY

IN 2 - AND 3 - SPACES



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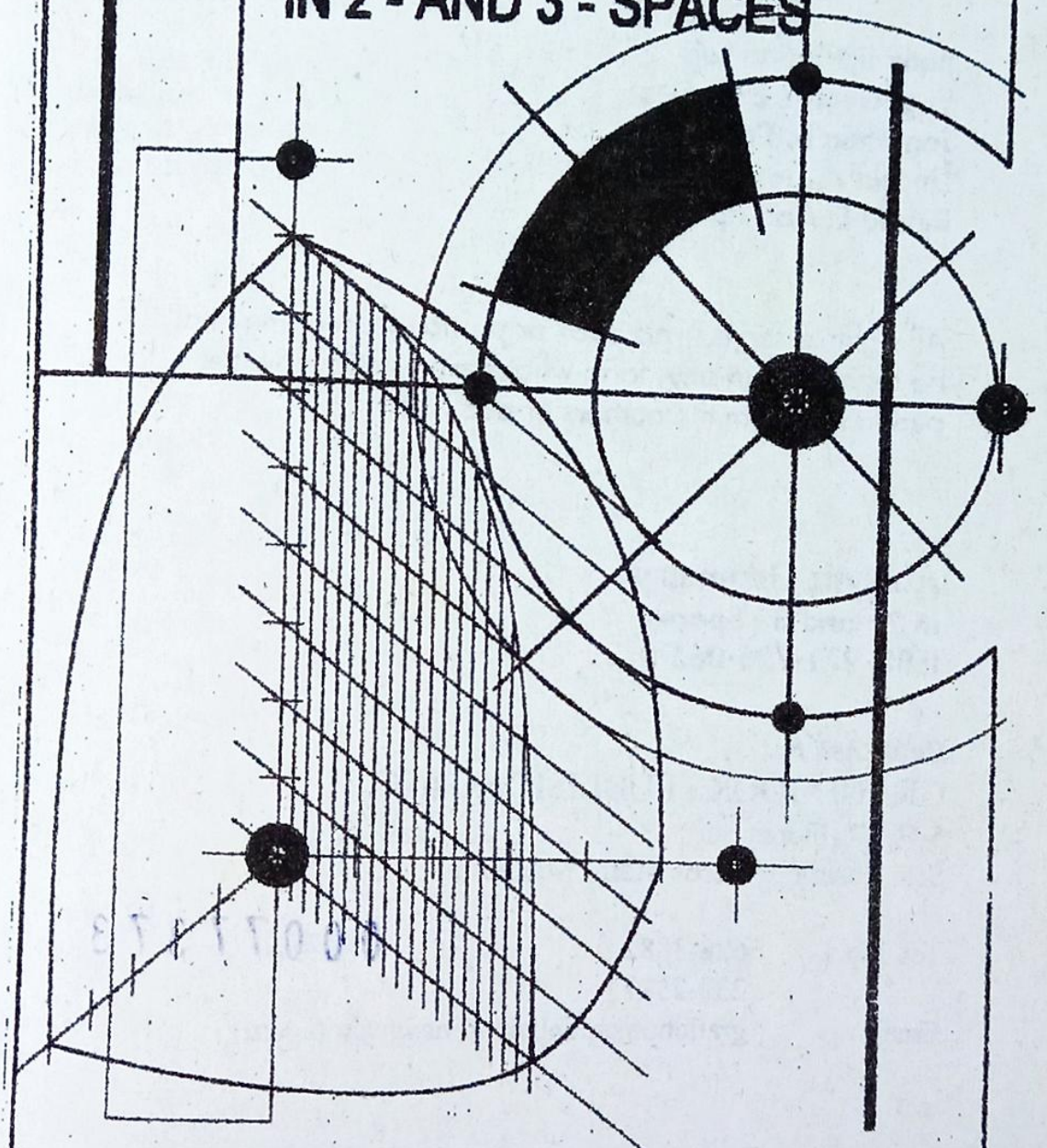

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Analytic Geometry
in 2 - and 3 - Spaces
ISBN 971-725-065-0

Published by:
GRANDBOOKS PUBLISHING INC.
50 M.R. Flores St.
Sto. Rosario, Pateros Metro Manila

Tel. No.: 628-3882
239-2587
Email: grandbookspublishinginc@yahoo.com

00077373

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