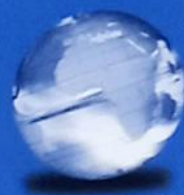


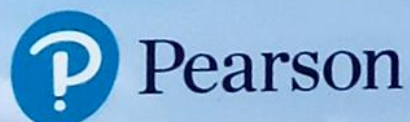
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# Modern Control Systems

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Richard C. Dorf • Robert H. Bishop



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Richard C. Dorf

University of California, Davis

Robert H. Bishop

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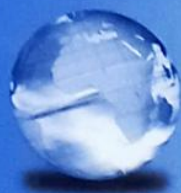
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