

CALCULUS OF A SINGLE VARIABLE

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RON LARSON

BRUCE EDWARDS

CALCULUS OF A SINGLE VARIABLE

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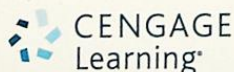
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Contents

P	▷ Preparation for Calculus	1
P.1	Graphs and Models	2
P.2	Linear Models and Rates of Change	10
P.3	Functions and Their Graphs	19
P.4	Review of Trigonometric Functions	31
	Review Exercises	41
	P.S. Problem Solving	43
1	▷ Limits and Their Properties	45
1.1	A Preview of Calculus	46
1.2	Finding Limits Graphically and Numerically	52
1.3	Evaluating Limits Analytically	63
1.4	Continuity and One-Sided Limits	74
1.5	Infinite Limits	87
	Section Project: Graphs and Limits of Trigonometric Functions	94
	Review Exercises	95
	P.S. Problem Solving	97
2	▷ Differentiation	99
2.1	The Derivative and the Tangent Line Problem	100
2.2	Basic Differentiation Rules and Rates of Change	110
2.3	Product and Quotient Rules and Higher-Order Derivatives	122
2.4	The Chain Rule	133
2.5	Implicit Differentiation	144
	Section Project: Optical Illusions	151
2.6	Related Rates	152
	Review Exercises	161
	P.S. Problem Solving	163

3	▷ Applications of Differentiation	165
3.1	Extrema on an Interval	166
3.2	Rolle's Theorem and the Mean Value Theorem	174
3.3	Increasing and Decreasing Functions and the First Derivative Test	181
	Section Project: Even Fourth-Degree Polynomials	190
3.4	Concavity and the Second Derivative Test	191
3.5	Limits at Infinity	199
3.6	A Summary of Curve Sketching	209
3.7	Optimization Problems	219
	Section Project: Minimum Time	228
3.8	Newton's Method	229
3.9	Differentials	235
	Review Exercises	242
	P.S. Problem Solving	245
4	▷ Integration	247
4.1	Antiderivatives and Indefinite Integration	248
4.2	Area	258
4.3	Riemann Sums and Definite Integrals	270
4.4	The Fundamental Theorem of Calculus	281
	Section Project: Demonstrating the Fundamental Theorem	295
4.5	Integration by Substitution	296
	Review Exercises	309
	P.S. Problem Solving	311
5	▷ Logarithmic, Exponential, and Other Transcendental Functions	313
5.1	The Natural Logarithmic Function: Differentiation	314
5.2	The Natural Logarithmic Function: Integration	324
5.3	Inverse Functions	333
5.4	Exponential Functions: Differentiation and Integration	342
5.5	Bases Other than e and Applications	352
	Section Project: Using Graphing Utilities to Estimate Slope	361
5.6	Indeterminate Forms and L'Hôpital's Rule	362
5.7	Inverse Trigonometric Functions: Differentiation	373
5.8	Inverse Trigonometric Functions: Integration	382
5.9	Hyperbolic Functions	390
	Section Project: Mercator Map	399
	Review Exercises	400
	P.S. Problem Solving	403

6	▷ Differential Equations	405
6.1	Slope Fields and Euler's Method	406
6.2	Growth and Decay	415
6.3	Separation of Variables and the Logistic Equation	423
6.4	First-Order Linear Differential Equations	432
	Section Project: Weight Loss	438
	Review Exercises	439
	P.S. Problem Solving	441
7	▷ Applications of Integration	443
7.1	Area of a Region Between Two Curves	444
7.2	Volume: The Disk Method	454
7.3	Volume: The Shell Method	465
	Section Project: Saturn	473
7.4	Arc Length and Surfaces of Revolution	474
7.5	Work	485
	Section Project: Pyramid of Khufu	493
7.6	Moments, Centers of Mass, and Centroids	494
7.7	Fluid Pressure and Fluid Force	505
	Review Exercises	511
	P.S. Problem Solving	513
8	▷ Integration Techniques and Improper Integrals	515
8.1	Basic Integration Rules	516
8.2	Integration by Parts	523
8.3	Trigonometric Integrals	532
	Section Project: The Wallis Product	540
8.4	Trigonometric Substitution	541
8.5	Partial Fractions	550
8.6	Numerical Integration	559
8.7	Integration by Tables and Other Integration Techniques	566
8.8	Improper Integrals	572
	Review Exercises	583
	P.S. Problem Solving	585

9 ▷ Infinite Series 587

- 9.1 Sequences 588
- 9.2 Series and Convergence 599
 - Section Project: Cantor's Disappearing Table** 608
- 9.3 The Integral Test and p -Series 609
 - Section Project: The Harmonic Series** 615
- 9.4 Comparisons of Series 616
- 9.5 Alternating Series 623
- 9.6 The Ratio and Root Tests 631
- 9.7 Taylor Polynomials and Approximations 640
- 9.8 Power Series 651
- 9.9 Representation of Functions by Power Series 661
- 9.10 Taylor and Maclaurin Series 668
 - Review Exercises** 680
 - P.S. Problem Solving** 683

10 ▷ Conics, Parametric Equations, and Polar Coordinates 685

- 10.1 Conics and Calculus 686
- 10.2 Plane Curves and Parametric Equations 700
 - Section Project: Cycloids** 709
- 10.3 Parametric Equations and Calculus 710
- 10.4 Polar Coordinates and Polar Graphs 719
 - Section Project: Cassini Oval** 728
- 10.5 Area and Arc Length in Polar Coordinates 729
- 10.6 Polar Equations of Conics and Kepler's Laws 738
 - Review Exercises** 746
 - P.S. Problem Solving** 749

Appendices

Appendix A: Proofs of Selected Theorems A2

Appendix B: Integration Tables A3

Appendix C: Precalculus Review (Online)*

Appendix D: Rotation and the General Second-Degree
Equation (Online)*

Appendix E: Complex Numbers (Online)*

Appendix F: Business and Economic Applications (Online)*

Appendix G: Fitting Models to Data (Online)*

Answers to All Odd-Numbered Exercises A7

Index A89

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