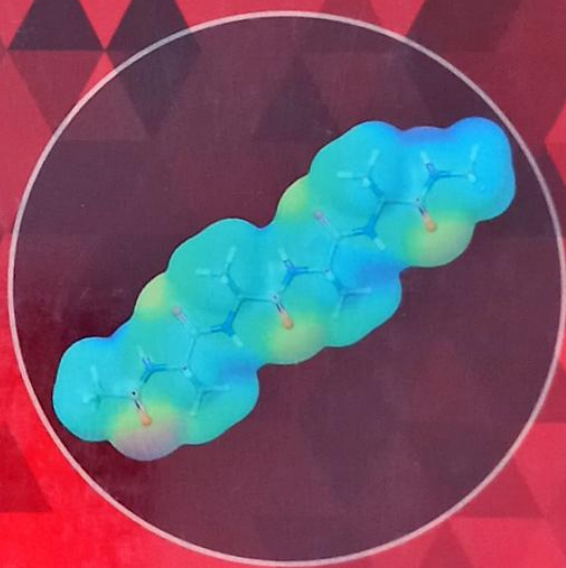


Third Edition

Introduction to **Computational Chemistry**



Frank Jensen

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Introduction to Computational Chemistry

Third Edition

Frank Jensen

Department of Chemistry, Aarhus University, Denmark

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Editorial Offices: 9600 Garsington Road, Oxford, OX4 2DQ, UK
The Atrium, Southern Gate, Chichester, West Sussex, PO19 8SQ, UK
111 River Street, Hoboken, NJ 07030-5774, USA

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Library of Congress Cataloging-in-Publication Data

Names: Jensen, Frank, author.

Title: Introduction to computational chemistry / Frank Jensen.

Description: Third edition. | Chichester, UK ; Hoboken, NJ : John Wiley & Sons, 2017. | Includes index.

Identifiers: LCCN 2016039772 (print) | LCCN 2016052630 (ebook) | ISBN 9781118825990 (pbk.) |

ISBN 9781118825983 (pdf) | ISBN 9781118825952 (epub)

Subjects: LCSH: Chemistry, Physical and theoretical—Data processing. | Chemistry, Physical and theoretical—Mathematics.

Classification: LCC QD455.3.E4 J46 2017 (print) | LCC QD455.3.E4 (ebook) | DDC 541.0285—dc23

LC record available at <https://lcn.loc.gov/2016039772>

A catalogue record for this book is available from the British Library.

ISBN: 9781118825990

Wiley also publishes its books in a variety of electronic formats. Some content that appears in print may not be available in electronic books.

Set in 10/12pt WarnockPro by Aptara Inc., New Delhi, India

Printed in Singapore by C.O.S. Printers Pte Ltd

10 9 8 7 6 5 4 3 2 1

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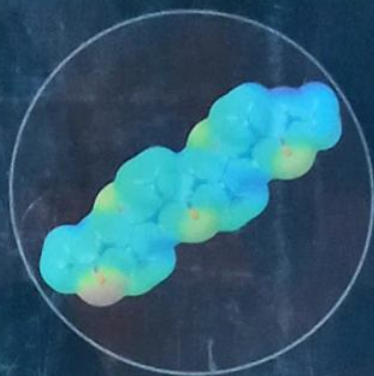
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Third Edition

Introduction to Computational Chemistry



FRANK JENSEN *Department of Chemistry, Aarhus University, Denmark*

Following on from the success of the second edition, *Introduction to Computational Chemistry, Third Edition*, provides an updated account of the fundamental principles underlying different methods, ranging from classical to sophisticated quantum models. Subjects covered include molecular structures and energetics, molecular properties, dynamic aspects, relative methods and qualitative models.

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An accessible introduction to the field, covering theory and practical aspects, this classic text is an invaluable guide for advanced undergraduates and graduate students entering the field of computational chemistry, as well as for professional researchers using computational methods as a tool for interpretations and designing new experiments and compounds.

FRANK JENSEN obtained his PhD from UCLA in 1987 with Professors C. S. Foote and K. N. Houk, and is currently an Associate Professor in the Department of Chemistry, Aarhus University, Denmark. He has published more than 150 papers and articles, and has made contributions to the widely used program package GAMESS.

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ISBN 978-1-118-82599-0



9 781118 825990