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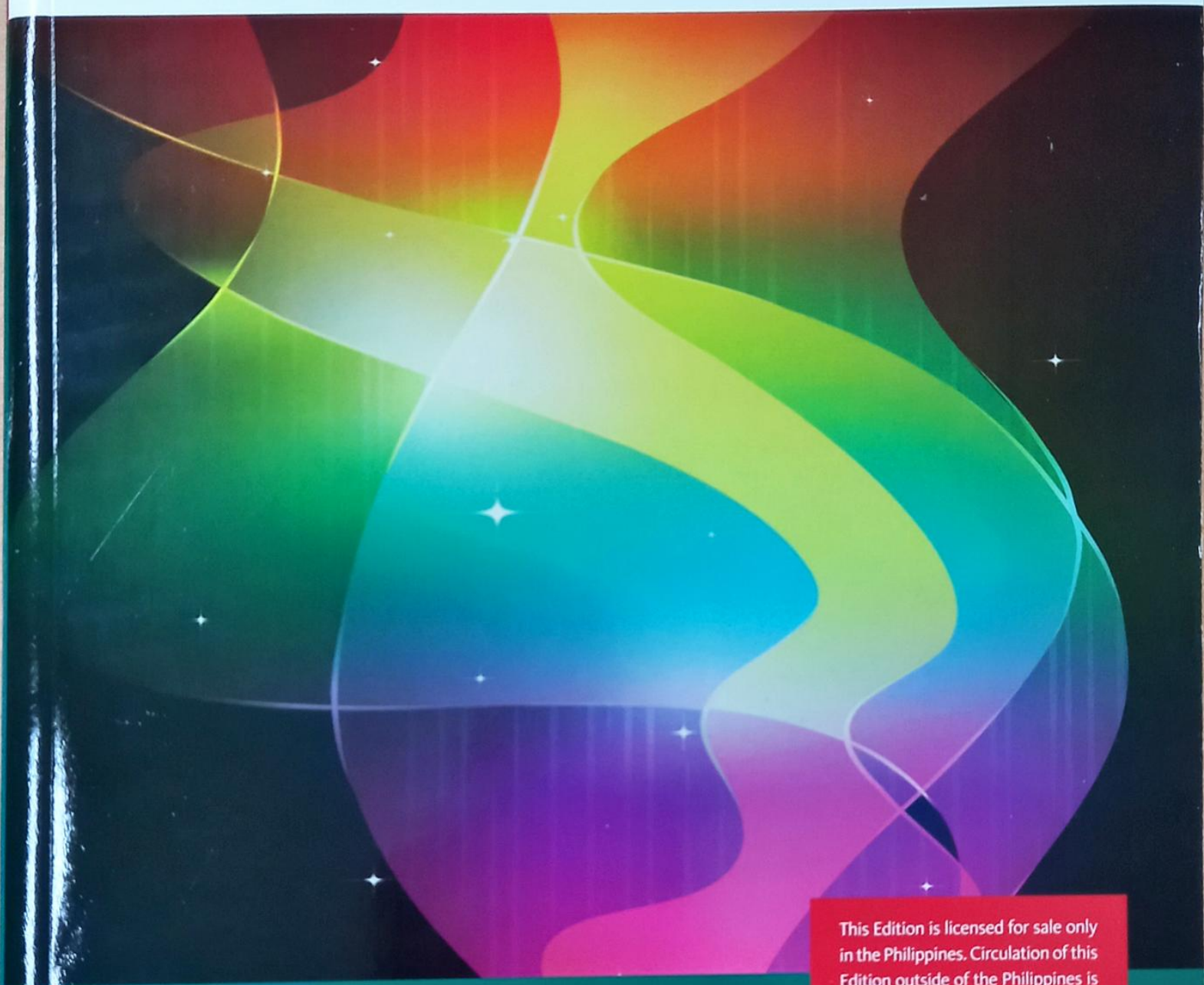

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Calculus

Eleventh Edition

Ron Larson • Bruce H. Edwards

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Bruce H. Edwards

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Calculus, 11th Edition

Ron Larson
Bruce H. Edwards

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Cengage Learning Asia Pte Ltd
151 Lorong Chuan
#02-08 New Tech Park
Singapore 556741

Cengage Learning Asia Pte Ltd (Philippines Branch)
Unit 1103, 11th Corporate Center
11th Avenue, corner Triangle Drive, North Bonifacio
Bonifacio Global City, Taguig City
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