

GLOBAL
EDITION



Calculus

*for Business, Economics, Life Sciences,
and Social Sciences*

FOURTEENTH EDITION

Raymond A. Barnett • Michael R. Ziegler
Karl E. Byleen • Christopher J. Stocker



fourteenth edition

CALCULUS

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Life Sciences, and
Social Sciences

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