

VECTOR MECHANICS for ENGINEERS

# STATICS | DYNAMICS

ELEVENTH EDITION

Beer • Johnston • Mazurek

Cornwell • Self

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Education

Eleventh Edition

# Vector Mechanics For Engineers

## Statics and Dynamics

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# VECTOR MECHANICS FOR ENGINEERS: STATICS AND DYNAMICS, ELEVENTH EDITION

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**A** first course in mechanics should develop a student's ability to analyze and solve problems using well-understood basic principles applied in a simple, logical manner. The emphasis of the 11<sup>th</sup> edition of *Vector Mechanics* continues this tradition and focuses on the correct understanding of the principles of mechanics and on their application to the solving of engineering problems. New to this edition, the text employs the **SMART Problem-Solving Methodology** in all Sample Problems. The SMART approach is used to consistently promote a systematic approach to solving engineering problems—**Strategy, Modeling, Analysis, and Reflect & Think**. The presentation and methodology is intended to support students applying this approach in all assigned problems. To further support student learning, practical applications are introduced early, new concepts are introduced simply, and fundamental principles are placed in simple contexts.

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